

# Strengthening of polyphase $\text{Si}_3\text{N}_4$ materials through oxidation

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Specimens of various polyphase  $\text{Si}_3\text{N}_4$  materials fabricated in the Si-Mg-O-N system, and a commercial  $\text{Si}_3\text{N}_4$  material were subjected to oxidation treatments prior to flexural strength determinations at  $1400^\circ\text{C}$ . It was demonstrated that a pre-oxidation treatment could significantly improve the high-temperature strength. The compositional change induced by oxidation which can decrease the volume fraction of the viscous phase present in these materials at high temperatures is believed to be responsible for the observed strengthening.

## 1. Introduction

The continuous glassy intergranular phase that exists in most (if not all) polycrystalline  $\text{Si}_3\text{N}_4$  materials plays an important role in both oxidation and mechanical property phenomena [1]. At high temperatures, this intergranular phase becomes viscous and both a path for fast diffusion [2] and a source of stress-induced cavitation. Oxidation phenomena take advantage of this continuous viscous phase for inward and outward diffusion of oxidation reactants and products [2]. The viscous phase is also responsible for mechanical property degradation at high temperatures. Under stress, it is a path for material rearrangement (diffusional creep) [3]. The propensity of the viscous phase to cavitate under stress is responsible for the slow-crack growth phenomena exhibited by polyphase  $\text{Si}_3\text{N}_4$  at high temperatures [4], and this is also responsible for its strength degradation.

Previous investigations have shown that oxidation resistance [2, 5] creep resistance [3] and high-temperature strength [5] of polyphase  $\text{Si}_3\text{N}_4$  fabricated in the Si-Mg-O-N system depend on its composition. All three of these properties decrease as the material's composition moves closer to the eutectic composition in the  $\text{Si}_3\text{N}_4$ - $\text{Si}_2\text{N}_2\text{O}$ - $\text{Mg}_2\text{SiO}_4$  compatibility triangle [6]. These observations strongly suggest that the volume fraction of the glassy intergranular phase,

which governs diffusional flux and cavitation propensity, is determined by the lever rule developed for determining phase content from phase diagrams. That is, the composition of the glassy phase is similar to the eutectic composition (i.e. the last liquid to solidify after fabrication) and its volume content depends on the bulk composition relative to the eutectic composition. Thus, within the limits of the compositions studied, the volume fraction of the glassy intergranular phase appears to increase as the bulk composition moves closer to the eutectic composition.

Discovery that the creep resistance of several different polyphase  $\text{Si}_3\text{N}_4$  materials could be improved by a pre-oxidation treatment [7, 8] was our first indication that the high-temperature strength may also be improved by the same treatment. During this same period, results of oxidation studies [2] had shown that compositional change is not only exhibited by the formation of a silicate surface scale, but also by a gradient of both the additive cation and the crystalline phases from the surface to the interior. As detailed elsewhere [2], the additive cation and cation impurities that reside in the glassy intergranular phase diffuse to the surface in an attempt to equilibrate the glass composition with the  $\text{SiO}_2$  formed by the oxidation of  $\text{Si}_3\text{N}_4$ . This outward diffusion forms a gradient of depleted additive (and impurity) cation(s). Oxygen, in the glassy phase originally



*Figure 1* Oxidized cross-section of a specimen previously oxidized at 1400° C/300 h. White film on parameter is the initial oxide scale. White centre is produced by a thin oxide scale formed on the less resistant composition. Darker zone illustrates the depth of compositional change which is more resistant to oxidation (specimen thickness = 0.3 cm).

associated with the outward diffusing cation(s), is left behind to react with  $\text{Si}_3\text{N}_4$  to form  $\text{Si}_2\text{N}_2\text{O}$ . The volume fraction of the glassy phase is thus reduced by the loss of both the outward moving cation(s) and the oxygen which reacts to form  $\text{Si}_2\text{N}_2\text{O}$ .<sup>\*</sup> Thus, the glassy intergranular phase is a fugitive of the oxidation process.

The compositional gradient produced by oxidation can best be visualized by the following demonstration. Oxidize a polyphase  $\text{Si}_3\text{N}_4$  specimen for a period sufficient to form a relatively thick surface scale. Section the specimen and re-expose the freshly cut surface to a much shorter oxidation period. Upon examination, the sectioned surface will reveal the compositional gradient due to the greater oxidation resistance (and thus thinner scale) of the cation depleted zone. An example is shown in Fig. 1 (initial composition (mole fractions): 0.755  $\text{Si}_3\text{N}_4$ , 0.120  $\text{SiO}_2$ , 0.125  $\text{MgO}$ ; oxidized for 300 h at 1400° C in air, sectioned and re-oxidized for 0.5 h at 1400° C). Quantitative microchemical and X-ray analysis of this same cross-section as presented elsewhere [2] also shows that the compositional change produced by oxidation extends to the centre of this specimen.

It was therefore concluded that since the detrimental glass phase can be a fugitive of the oxidation process, oxidation could improve the high temperature mechanical properties as first discovered during creep experiments and as it will now be demonstrated through strength measurements.

## 2. Experimental procedure

The object of this study was to determine the effect of a pre-oxidation treatment on the high-temperature strength of polyphase  $\text{Si}_3\text{N}_4$ . Materials fabricated in the Si–Mg–O–N system were chosen for this study. Since prolonged oxidation is known to produce surface pits in these materials [9, 10] which introduce a detrimental, new flaw population, pre-oxidized specimens were reground to remove the surface pits prior to strength determinations.

The first group of bar specimens examined were diamond cut and ground from 19 different materials which form three series of compositions previously investigated at high temperatures in studies concerning strength [5], creep [3], and oxidation resistance [2]. Materials in each series contained a fixed mole fraction of  $\text{Si}_3\text{N}_4$  (either 0.91, 0.833 or 0.755) and a given  $\text{MgO}/\text{SiO}_2$  molar ratio that could range between 0.1 and 11. Fabrication details have been presented elsewhere [5]. All 19 specimens were placed on a reaction-bonded  $\text{Si}_3\text{N}_4$  setter with raised knife-edge contacts and oxidized together in air at 1400° C for 300 h. The specimens were weighed before and after oxidation, each specimen was separately surface ground until surface pits, formed to various depths on the different materials, were no longer observed by visual inspection with a binocular microscope.

The second group of specimens were cut from a large billet of commercial, hot-pressed  $\text{Si}_3\text{N}_4$  (NC 132) obtained recently from the Norton Company, which is also fabricated in the Si–Mg–O–N system. This group was separated into different sets. Flexural strength measurements were made at room temperature and 1400° C without a pre-oxidation treatment. The other sets were subjected to oxidation in air at either 1400 or 1500° C for various periods prior to regrinding and strength determinations at either room temperature or 1400° C. The amount of material removed by regrinding was dependent on the depth of the surface pits formed during oxidation as discussed above.

All flexural testing was performed on bar specimens (approximate dimensions of 0.3 cm × 0.6 cm × 3.2 cm) using a four-point loading device with inner and outer spans of 1.27 and 2.54 cm,

<sup>\*</sup>Equilibrium considerations require that the viscous phase maintain its original composition. That is, a portion of the  $\text{SiO}_2$  in the viscous phase reacts with the  $\text{Si}_3\text{N}_4$  to produce  $\text{Si}_2\text{N}_2\text{O}$ .

TABLE I Oxidation and strength data for Si-Mg-O-N compositions oxidized at 1400° C/300 h

Initial composition (mole fraction)			MgO/SiO <sub>2</sub> molar ratio	Weight change (mg cm <sup>-2</sup> )	Flexural strength (MPa)	Prior flexural strength (MPa)	Change (%)
Si <sub>3</sub> N <sub>4</sub>	MgO	SiO <sub>2</sub>					
0.910	0.020	0.070	0.29	0.93	482	343	+ 40
0.910	0.030	0.060	0.50	1.36	534	339	+ 57
0.910	0.040	0.050	0.80	1.74	445	307	+ 45
0.910	0.055	0.035	1.57	1.78	327	183	+ 79
0.910	0.065	0.025	2.60	2.39	500	269	+ 86
0.833	0.015	0.152	0.10	0.21	452	287	+ 58
0.833	0.030	0.137	0.22	1.40	420	352	+ 19
0.833	0.040	0.127	0.31	2.09	319	341	- 7
0.833	0.052	0.110	0.47	2.02	452	334	+ 35
0.833	0.085	0.082	1.04	3.34	377	211	+ 79
0.833	0.120	0.047	2.55	5.31	350	280	+ 25
0.833	0.144	0.023	6.26	4.72	411	476	- 14
0.755	0.020	0.225	0.09	0.93	405	225	+ 80
0.755	0.055	0.190	0.29	1.92	455	269	+ 69
0.755	0.085	0.160	0.53	3.18	449	279	+ 61
0.755	0.125	0.120	1.04	4.30	338	199	+ 70
0.755	0.155	0.090	1.72	4.41	510	193	+ 164
0.755	0.190	0.055	3.45	4.47	500	414	+ 21
0.755	0.225	0.020	11.25	5.94	324	408	- 16

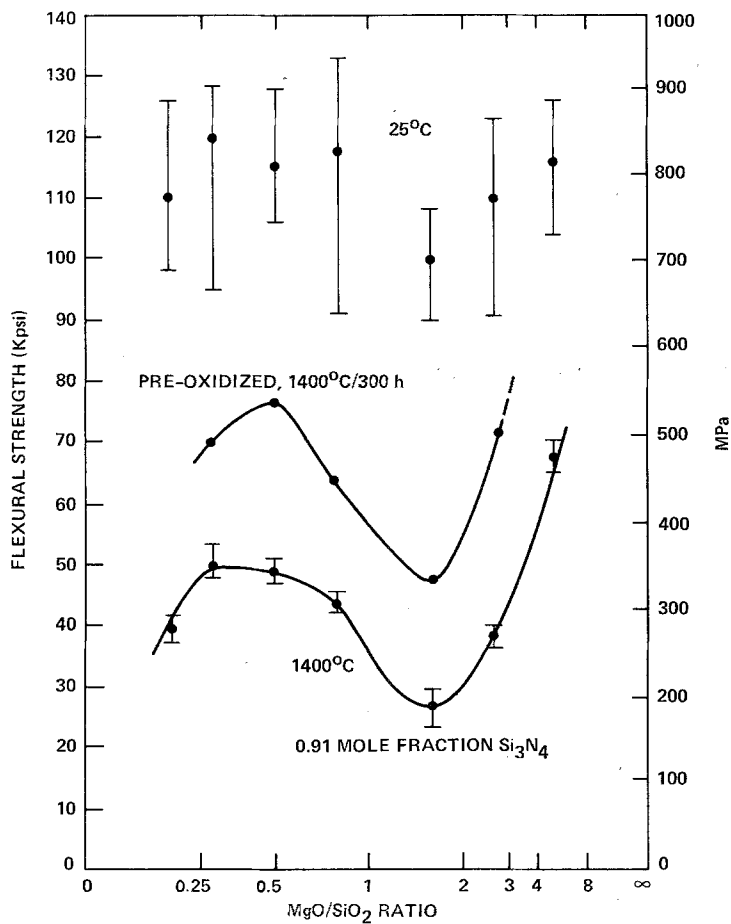


Figure 2 Flexural strength data for the series containing 0.91 mole fraction Si<sub>3</sub>N<sub>4</sub> fabricated with different MgO/SiO<sub>2</sub> molar ratios. Data include the 5 specimens subjected to a 1400° C/300 h pre-oxidation treatment.

respectively and a crosshead speed of  $0.05 \text{ cm min}^{-1}$ . X-ray diffraction analysis was used to determine the crystalline phase content of the surfaces of the unoxidized and oxidized, reground specimen. The intensity ratio of (1 1 1)  $\text{Si}_2\text{N}_2\text{O}$  and (2 0 0)  $\text{Si}_3\text{N}_4$  diffraction peaks determined by an area analysis was used to report compositional changes.

### 3. Results

#### 3.1. Compositions with various MgO/SiO<sub>2</sub> ratios

Table I lists the specimens, their initial compositions, their weight gain during oxidation per unit area, and their flexural strengths ( $1400^\circ\text{C}$  in air) after the  $1400^\circ\text{C}/300 \text{ h}$  oxidation treatment. The second from last column lists the per cent change in strength due to the pre-oxidation treatment. Fig. 2 illustrates, for comparative purposes, the strength data (room temperature,  $1400^\circ\text{C}$ , and pre-oxidized,  $1400^\circ\text{C}$ ) for the series containing 0.91 mole fraction  $\text{Si}_3\text{N}_4$ .

Both Table I and Fig. 2 illustrate that a pre-oxidation treatment can significantly improve the high-temperature strength of polyphase  $\text{Si}_3\text{N}_4$  materials. Within each series, the largest increase occurs for compositions with a MgO/SiO<sub>2</sub> molar ratio between 1 and 3. Also, compositions with MgO/SiO<sub>2</sub> > 4 exhibit a strength decrease after oxidation.

Flexural strength calculations assumed an elastic stress-strain behaviour. Data obtained previously for unoxidized specimens tested at  $1400^\circ\text{C}$  with an MgO/SiO<sub>2</sub> ratio ranging between 1 to 3 exhibited a nonelastic behaviour upon stressing to failure, indicative of lower strengths than reported in Table I and Fig. 2. On the other hand, all pre-oxidized specimens did exhibit an elastic stress-strain response to failure. Thus, the strength difference for compositions within this range of MgO/SiO<sub>2</sub> ratios is even greater than that reported in Table I.

Fig. 3 shows the  $\text{Si}_2\text{N}_2\text{O}/\text{Si}_3\text{N}_4$  ratio determined on ground surfaces of both unoxidized ( $1400^\circ\text{C}/300 \text{ h}$ ) specimens. This ratio is plotted as a function of the initial MgO/SiO<sub>2</sub> molar ratio. Data for the unoxidized specimens are representative of the material's bulk. But because oxidation produces a gradient in the  $\text{Si}_2\text{N}_2\text{O}/\text{Si}_3\text{N}_4$  ratio [2], data for specimens subjected to oxidation are only representative of the depth for which material was removed by grinding to eliminate surface pits.

Although data for the oxidized specimens are not representative of its bulk, it does show that compositional changes as outlined in the introduction did take place, i.e. the average bulk composition decreases its MgO/SiO<sub>2</sub> ratio shifts toward the  $\text{Si}_3\text{N}_4$ - $\text{Si}_2\text{N}_2\text{O}$  tie line. Note that the larger changes occur for materials with an initial MgO/SiO<sub>2</sub> molar ratio between 0.5 and 3.0.

#### 3.2. Commercial $\text{Si}_3\text{N}_4$ material

Table II lists the oxidation treatments for the specimens of NC 132. As shown, most of the specimens were subjected to various periods of oxidation at  $1400^\circ\text{C}$  prior to regrinding and strength testing. After it was discovered that excessive periods (> 500 h) at  $1400^\circ\text{C}$  were required to achieve modest strength gains at high temperatures, the remaining specimens were oxidized at  $1500^\circ\text{C}$ . As indicated in Table II, significant strengthening can be achieved by a pre-oxidation treatment at  $1500^\circ\text{C}$ . It was also demonstrated that such a treatment did not impair the room temperature strength. A detailed description of these results now follows.

Flexural strength measurements of unoxidized specimens at 25 and  $1400^\circ\text{C}$  resulted in an average strength of 878 and 282 MPa, respectively. The load-deflection response of these specimens at  $1400^\circ\text{C}$  was nonlinear indicating extensive creep during strength testing. Although the strength of these specimens at  $1400^\circ\text{C}$  is listed as 282 MPa, the authors recognize that the material's true strength could be significantly lower due to the extensive creep and the use of an elastic solution to calculate strength [11]. In addition, the area of subcritical crack growth could easily be distinguished as previously reported [12], i.e. the fracture area traversed by the slowly moving crack can be distinguished by the rougher topography caused by extensive cavitation.

Short periods of oxidation (50 h) prior to strength testing resulted in a nearly linear load-deflection response. After a pre-oxidation period of 100 h, the load-deflection response was linear to fracture. Judging the first results obtained on the materials fabricated by the authors, high-temperature strengthening was expected for oxidation periods of  $\sim 300 \text{ h}$  at  $1400^\circ\text{C}$ . But contrary to this expectation, modest strengthening was not observed until the oxidation period at  $1400^\circ\text{C}$  was increased to 548 h. It then became obvious that significant strengthening could be

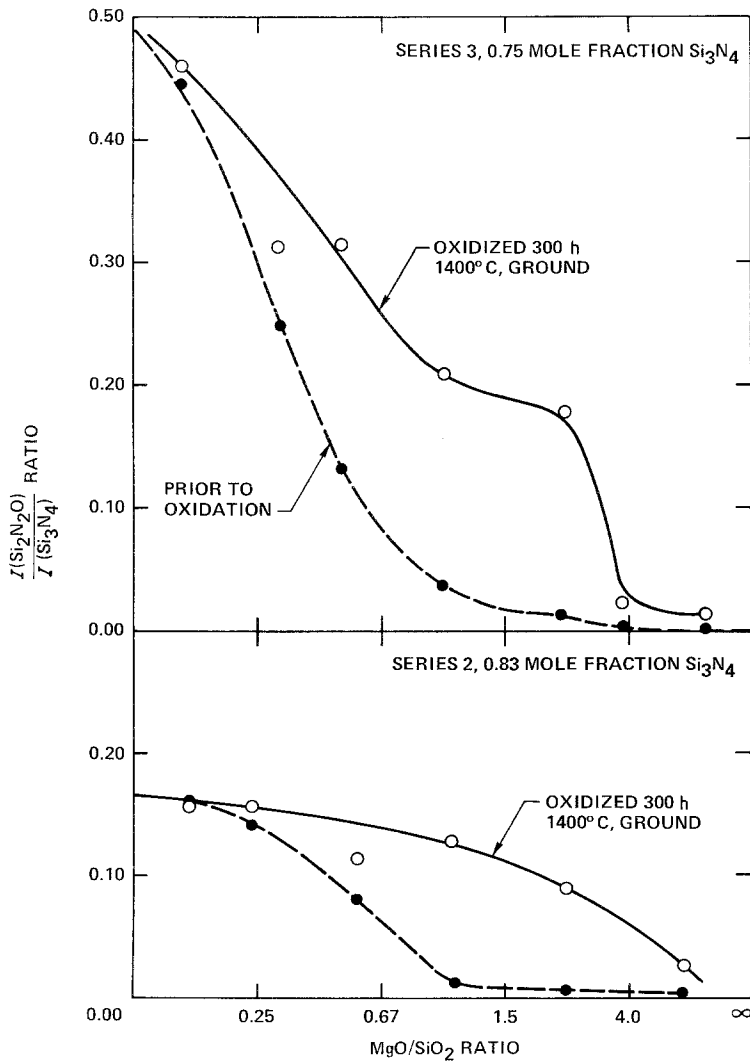


Figure 3 Ratio of X-ray diffraction intensities of  $\text{Si}_2\text{N}_2\text{O}$  and  $\text{Si}_3\text{N}_4$  prior to and after the  $1400^\circ\text{C}/300\text{ h}$  pre-oxidation treatment as plotted against the initial  $\text{MgO}/\text{SiO}_2$  molar ratio.

TABLE II Flexural strength results for commercial  $\text{Si}_3\text{N}_4$

Oxidation treatment		Test temperature ( $^\circ\text{C}$ )	Number	Weight gain/area ( $\text{mg cm}^{-2}$ )	Depth removed (cm)	Average strength (MPa)	Weight parameters	
Temperature ( $^\circ\text{C}$ )	Time (h)						$m$	$\sigma_0$ (MPa)
None	None	25	7	—	—	878	8	924
None	None	1400	8	—	—	282	( $\pm 4\%$ ) <sup>†</sup>	
1400	50	1400	3	1.61	0.015	254	( $\pm 4\%$ )	
1400	100	1400	3	2.13	0.020	256	( $\pm 7\%$ )	
1400	256	1400	4	—	—	288	( $\pm 8\%$ )	
1400	332	25	8	2.39	0.020	982	15	1014
1400	332	1400	8	2.39	0.020	280	24	286
1400	548	1400	3	—*	0.020	376	( $\pm 5\%$ )	
1500	206	25	7	—*	0.050	805	11	834
1500	206	1400	7	—*	0.050	482	17	496
1500	306	1400	5	—*	0.050	571	( $\pm 3\%$ )	

\*Scale flaked off during oxidation.

<sup>†</sup>Numbers in brackets denote per cent difference of either maximum or minimum strength values from the average.

achieved within a more reasonable period by increasing the oxidation kinetics by increasing the oxidation temperature. It was thus demonstrated that a pre-oxidation treatment of 300 h at 1500°C could raise the 1400°C strength of NC 132 from < 30% to 70% of its room temperature value. It is expected that longer periods at 1500°C or higher temperatures will result in further strengthening.

Another objective was to determine if the pre-oxidation treatment might influence the lower temperature strengths. As indicated in Table II, room temperature strength measurements were obtained with reground specimens after oxidation treatments of 1400°C/332 h and 1500°C/206 h. Data obtained after the 1400°C/332 h treatment indicates a modest strengthening (~12%), and as shown in Fig. 4, a narrower strength distribution. As shown in Fig. 4, the 1500°C/206 h treatment resulted in a strength distribution similar to that obtained at room temperature for specimens that were not subjected to a pre-oxidation treatment.

Fig. 4 also reports the Weibull strength statistics of the high-temperature data where a linear load-deflection response was observed. Table II reports the two Weibull parameters for these data. As indicated, minimal strength scatter is observed for all high-temperature results. This is indicative of slow-crack growth as first pointed out by Charles [13]. It should be noted that although slow-crack growth was prevalent at high tempera-

tures, the fracture surface did not reveal any topographical difference between the slow and fast crack growth regions.

Attempts were made to obtain oxidation kinetics through weight change measurements. As shown in Table II, data was limited to the shorter periods at 1400°C. The oxide scale flaked off at longer periods and during the 1500°C treatments. Table II also shows that the surface pits were deeper for longer oxidation periods or higher temperatures. One oxidized specimen (1400°C/332 h) tested at 1400°C without regrinding resulted in a strength of 165 MPa. This much lower strength was due to fracture initiating at a deep surface pit.

The X-ray diffraction analysis results obtained from the ground surfaces of specimens subjected to various oxidizing treatments are shown in Fig. 5. Conversion of the Si<sub>2</sub>N<sub>2</sub>O/Si<sub>3</sub>N<sub>4</sub> intensity ratio to weight per cent Si<sub>2</sub>N<sub>2</sub>O was carried out according to the calibrated method described by Mencik and Short [14]. This analysis, as used here, assumed no other phase present other than either Si<sub>2</sub>N<sub>2</sub>O or Si<sub>3</sub>N<sub>4</sub>. As shown in Fig. 5, the Si<sub>2</sub>N<sub>2</sub>O content increases rapidly for short periods of oxidation at 1400°C and then levels off at longer periods. Oxidation at 1500°C promotes a greater compositional change.

#### 4. Discussion

As detailed above, the high-temperature strength of polyphase Si<sub>3</sub>N<sub>4</sub> materials can be significantly

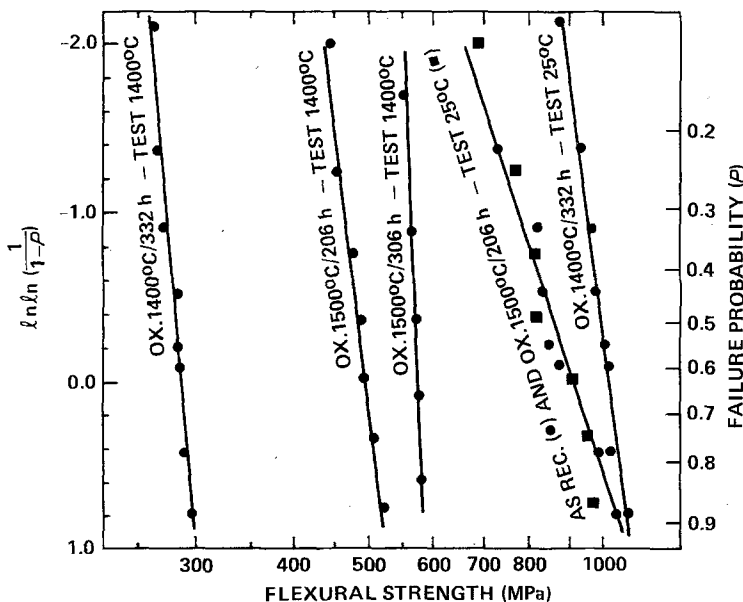


Figure 4 Statistics for the flexural strength data of NC132 Si<sub>3</sub>N<sub>4</sub> material subjected to different pre-oxidation treatments.

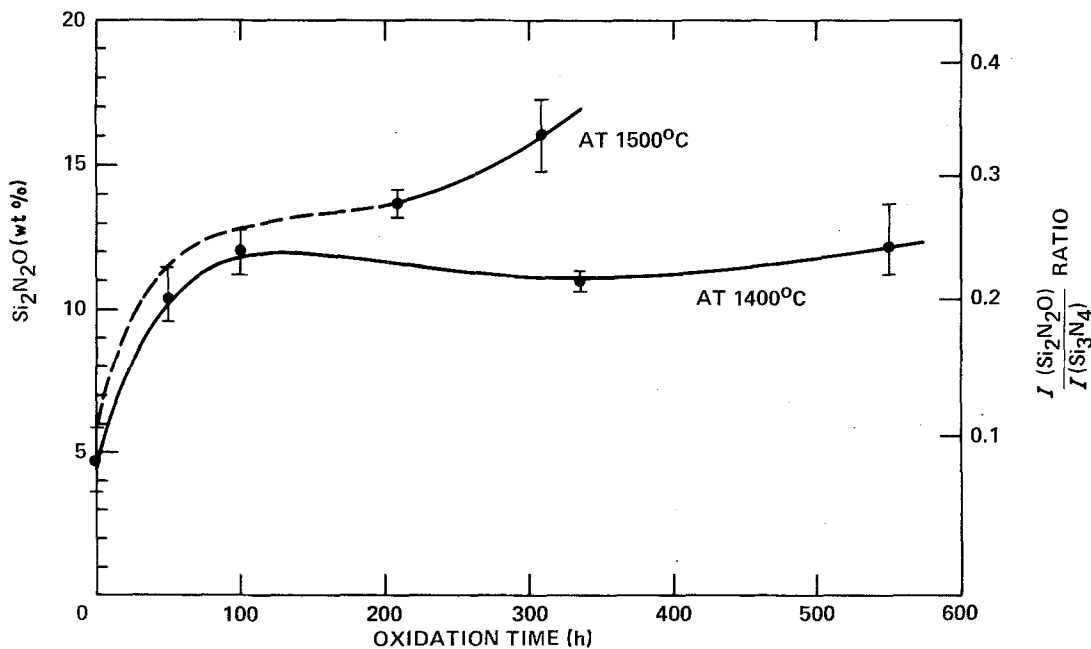


Figure 5 Si<sub>2</sub>N<sub>2</sub>O content of NC 132 reground surfaces subjected to pre-oxidation treatments at 1400 and 1500°C as a function of treatment period.

improved by an oxidation treatment. For the system chosen for examination here, which develops surface pits during oxidation due to localized surface reactions with iron-type inclusions [10], surface regrinding is necessary to realize these strength improvements. It is expected that for other material systems that do not exhibit surface pitting (e.g. materials in the Si<sub>3</sub>N<sub>4</sub>-Si<sub>2</sub>N<sub>2</sub>O-Y<sub>2</sub>Si<sub>2</sub>O<sub>7</sub> system), regrinding may not be necessary.

The strength improvements can be related to the compositional changes induced by oxidation. Oxidation shifts the average bulk composition toward Si<sub>2</sub>N<sub>2</sub>O. This compositional shift changes the volume content of the liquid in equilibrium with the crystalline phases. Most of the materials studied here had initial compositions within the Si<sub>3</sub>N<sub>4</sub>-Si<sub>2</sub>N<sub>2</sub>O-Mg<sub>2</sub>SiO<sub>4</sub> compatibility triangle, which contains the lowest melting eutectic of the two compatibility triangles in which Si<sub>3</sub>N<sub>4</sub> is an equilibrium phase [6]. For these materials any compositional shift toward the Si<sub>3</sub>N<sub>4</sub>-Si<sub>2</sub>N<sub>2</sub>O tie line will decrease the volume content of the eutectic melt and thus result in a strengthening. On the other hand, for compositions in the Si<sub>3</sub>N<sub>4</sub>-Mg<sub>2</sub>SiO<sub>4</sub>-MgO compatibility triangle (MgO/SiO<sub>2</sub> > 2), a small compositional shift toward the Si<sub>3</sub>N<sub>4</sub>-Si<sub>2</sub>N<sub>2</sub>O tie line would move the composition into the Si<sub>3</sub>N<sub>4</sub>-Si<sub>2</sub>N<sub>2</sub>O-Mg<sub>2</sub>SiO<sub>4</sub> compatibility triangle to increase the volume

fraction of the eutectic melt (and therefore the residual glass phase) and thus result in a strength decrease. This is observed for the two materials in series 2 and 3 (Table I) with the highest initial MgO/SiO<sub>2</sub> ratios. Further oxidation resulting in a greater compositional shift should produce a strengthening for these two materials.

The extent of the oxidation required to produce a desired strengthening will depend on the material's initial composition, which controls its initial oxidation kinetics [5], and on temperature, which also controls oxidation kinetics. Impurities must also be included in considering the material's composition. Impurities not only help govern the eutectic composition, its melting temperature and its volume fraction, but they can also diffuse to the surface during oxidation [2]. Thus a specific oxidation treatment scheduled, cannot be presently recommended for an arbitrary composition without analytical relations between oxidation kinetics, compositional change and residual glass phase contents.

The question of to what depth from the surface an oxidation treatment can produce the compositional change required for significant strengthening has not been answered here. Previous experiments [2] involving quantitative compositional measurements show that for specimens of the size used here (~0.3 cm thick), a significant compositional change does occur at the centre

of the specimen after  $\sim 300$  h at  $1400^\circ\text{C}$ . For the specimens treated here, the thickness was reduced by 15 to 35% by surface grinding. Judging from the compositional profiles obtained from the previous studies, it appears that much of the steep portion of the compositional gradient was removed. This suggests that the compositional changes reported in Figs. 3 and 5 are nearly representative of the specimen's centre.

Another interesting result was the slight strengthening obtained at room temperature after the  $1400^\circ\text{C}/332$  h treatment. Oxidation reactions produce both molar volume changes and compositional gradients. Either one or both of these phenomena will produce residual surface stresses as detailed experimentally in the Appendix. The reaction  $2\text{Si}_3\text{N}_4 + 1.5 \text{O}_2 \rightarrow 3\text{Si}_2\text{N}_2\text{O} + \text{N}_2$  results in a molar volume increase of  $\sim 20\%$ . Although most of the compressive stresses produced by this volume increase are expected to relax during oxidation, some remain to produce the apparent room temperature strengthening observed after the  $1400^\circ\text{C}/332$  h treatment.

In conclusion, it has been shown that a pre-oxidation treatment can significantly increase the high-temperature mechanical properties of dense, polyphase  $\text{Si}_3\text{N}_4$  without affecting their low-temperature strength. Oxidation resistance is also significantly improved by this treatment. This observation suggests that  $\text{Si}_3\text{N}_4$  compositions

that can easily be sintered because of a large amount of a liquid phase, but have poor high-temperature properties, can be improved by a post-fabrication oxidation treatment.

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### Appendix: Surface compressive stresses arising during oxidation of $\text{Si}_3\text{N}_4$

As documented elsewhere [15], the compressive surface stresses which arise due to molar volume changes accompanying oxidation can be qualitatively assessed by measuring the apparent critical stress intensity factor with an indentation technique. The apparent critical stress intensity factor ( $K_a$ ) is proportional to the magnitude of the compressive surface stress and the depth to which this stress extends into the material.

Polished specimens of a  $\text{Si}_3\text{N}_4$  material ( $0.833 \text{Si}_3\text{N}_4$ ,  $\text{MgO}/\text{SiO}_2 = 2.55$ ) were oxidized for different periods at  $1400^\circ\text{C}$ . The friable outer scale was removed by light sand-blasting. Indentations were made (20 kg) at room temperature to obtain  $K_a$  of the sub-scale surface material. The results illustrated in Fig. A1 show that compressive

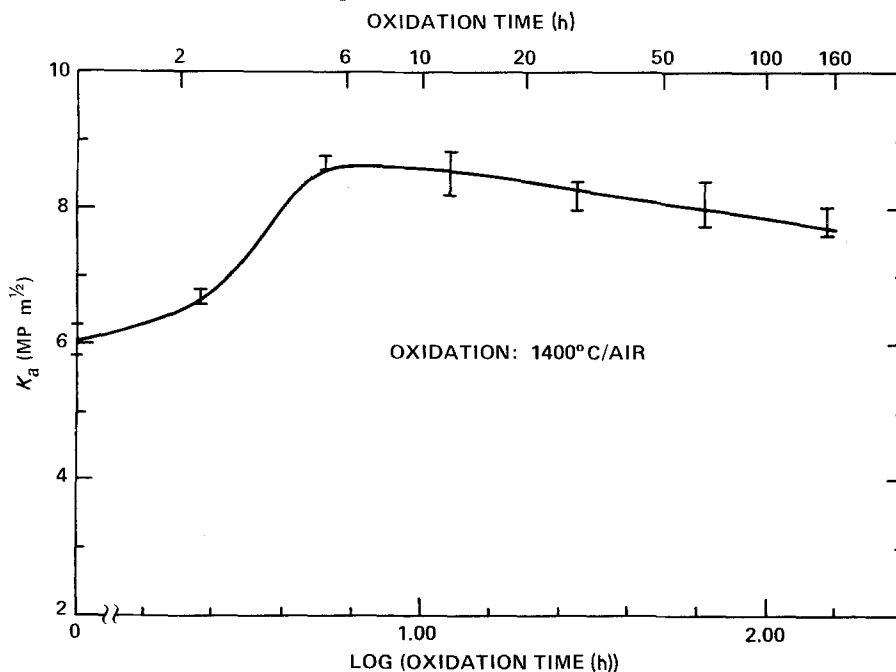


Figure A1 Apparent critical stress intensity factor against oxidation period at  $1400^\circ\text{C}$ .



stresses do arise during oxidation, namely, within a period of  $\sim 5$  h,  $K_a$  increases from 6 to  $8.7 \text{ MPa m}^{1/2}$ . As oxidation proceeds beyond 5 h,  $K_a$  decreases from its maximum value consistent with the observation (see text) that the compositional gradient (one factor that governs the magnitude of the compressive stress) decreases with increasing oxidation time.

It can be concluded that compressive stresses do develop in the sub-scale material due to oxidation. One might suspect that the large molar volume increase (21.5%) due to the oxidation of  $\text{Si}_3\text{N}_4$  to  $\text{Si}_2\text{N}_2\text{O}$  could be responsible for these compressive surface stresses, most of which are relieved by creep during oxidation. Since the thermal expansion of  $\text{Si}_2\text{N}_2\text{O}$  (the predominant sub-scale phase) is greater than that of  $\text{Si}_3\text{N}_4$ , one could rule out thermal expansion mismatch as a cause for the compressive surface stresses.

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